

# Design of Reconfigurable Predictive Control Applied to the Air Path of a Diesel Engine

Khaoula Layerle, Nicolas Langlois, Houcine Chafouk

*Institut de Recherche en Systèmes Electroniques Embarqués (IRSEEM), Technopôle du Madrillet, Avenue Galilée - BP 10024, 76801 Saint Etienne du Rouvray Cedex France. (Tel: +332 32 91 58 23; e-mails: khaoula.layerle@esigelec.fr, langlois@esigelec.fr)*

**Abstract:** In this paper, a method for reconfigurable predictive control of the air path of a Diesel engine system is presented. Failures are identified indirectly by estimating the parameters of the linear engine model using the recursive least squares algorithm (RLS). The actuators of the air system considered here are a variable geometry turbine (VGT) and an exhaust gas recirculation valve (EGR). The aim of the reconfiguration controller is to track simultaneously the desired trajectories of intake pressure ( $P_1$ ) and exhaust pressure ( $P_2$ ) when faults occur. Some simulation results are presented and compared to Generalized Predictive Control (GPC) applied on the coupled Multi-Input, Multi-Output (MIMO) system. The proposed controller exhibits good control performance: it ensures global stability and tracking of output references without zero offset. Moreover, separating the optimization of the GPC parameters for each subsystem permits the controller to have good performance during transient mode especially in terms of overshoots.

Keywords: GPC, non-minimum phase system, Re-configuration, Diesel engine.

## 1. INTRODUCTION

For several years the industrial community has expressed a growing interest in reliability, safety, and durability of dynamic systems. This is why significant research in Fault Detection and Isolation (FDI) was widely treated in Chen and Patton (1999). Unfortunately, little attention was paid to the subsequent problem, i.e., Fault-Tolerant Control (FTC) until the mid 1980s, Looze et al. (1985). More recently, FTC problem has begun to draw more attention, Patton (1997), Huzmezan and Maciejowski (1997) and Benbouzid et al. (2007).

There has always been interest in GPC which has significantly influenced process control, Qin and Badgwell (2003). This type of control continues to be the subject of many theoretical works aiming to extend its potential fields of applications. Optimization under constraints and control of non-minimum phase MIMO systems are among the main issues studied in the literature, Watanabe et al. (1991), Ricker (1991) and Mayne et al. (2000). The introduction of flatness in GPC based on output approach theory has made this problem solvable, Fliess and Marquez (2000), Plianos et al. (2007).

This paper describes a method to design GPC dedicated to unstable non-minimum phase systems, Layerle et al. (2007). Requiring access to all state variables of a given system, the proposed design approach necessitates the use of an observer.

Since the observer parameters must be re-estimated when an actuator or /and system fault occurs, the indirect failure accommodation method is applied, Noura et al. (1994). Such an approach permits the control law parameters to be updated. The functionality and safety of the system are

thus maintained.

This paper is organized as follows : in section 2 a brief description of the system to be controlled is given. In section 3 the GPC state-space approach and its instability problem are briefly described. In section 4 the development of the predictive controller is given. Some simulation results are given in section 5 and section 6 concludes the paper.

## 2. SYSTEM DESCRIPTION

The nomenclature of the Diesel engine variables are given in the following table. The Diesel engine configuration is schematically given in (Fig. 1). The seven-order mean-

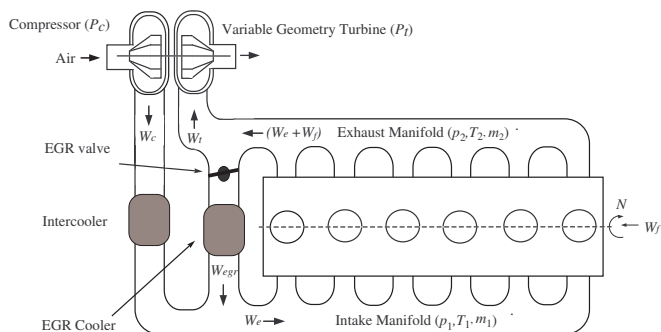


Fig. 1. Air system of Diesel engine

value model of the Diesel engine equipped with a VGT and an EGR valve in Jankovic et al. (2000) is considered. In order to reduce the system order, some hypotheses are considered as proposed in Jankovic et al. (2000):

Nomenclature	
Variable	Description
$EGR$	Exhaust Gas Recirculation
$AFR$	Air Fuel Ratio
$N$	Engine speed
$F_1$	Intake manifold burned gas fraction
$F_2$	Exhaust manifold burned gas fraction
$m_1$	Mass of gas in the intake manifold
$m_2$	Mass of gas in the exhaust manifold
$p_1$	Gas pressure in the intake manifold
$p_2$	Gas pressure in the exhaust manifold
$P_c$	Compressor power
$P_t$	Turbine power
$W_e$	Total mass flow rate into the engine
$W_c$	Compressor mass flow rate
$W_t$	Turbine mass flow rate
$W_f$	Fuel mass flow rate
$W_{egr}$	EGR mass flow rate
$V_1$	Intake manifold volume
$V_2$	Exhaust manifold volume
$T_1$	Intake manifold temperature
$T_2$	Exhaust manifold temperature
$T_c$	Compressor temperature
$T_e$	Temperature of the exhaust from the engine
$T_{egr}$	EGR temperature
$\omega_{tc}$	Turbocharger speed
$J_{tc}$	Turbocharger moment of inertia
$\eta_c$	Compressor isentropic efficiency
$\eta_t$	Turbine isentropic efficiency
$\eta_m$	Turbocharger mechanical efficiency
$\gamma$	Specific heat ratio
$R$	Specific gas constant

- The fraction of burned gas in the intake and exhaust manifold  $F_1$  and  $F_2$  are removed from the model because they are difficult to measure.
- The mass of gas in intake and exhaust manifold  $m_1$  and  $m_2$  are removed from the model, because they are difficult to control.
- The turbocharger dynamics is modeled as a first-order lag power transfer with time constant  $\tau$ .

For the developed below method, we are interested in a Diesel engine model with three state variables described as follows:

$$\begin{aligned}\dot{p}_1 &= k_1(W_c + W_{egr} - k_e p_1) + \frac{\dot{T}_1}{T_1} p_1 \\ \dot{p}_2 &= k_2(k_e p_1 - W_{egr} - W_t + W_f) + \frac{\dot{T}_2}{T_2} p_2 \\ \dot{P}_c &= \frac{1}{\tau}(\eta_m P_t - P_c)\end{aligned}\quad (1)$$

where  $k_i$  is the coefficient of the first law  $k_i = \frac{RT_i}{V_i}$  and  $k_e = k_e(N, T_1)$ .  $T_1$  and  $T_2$  are supposed constant during the following statements.  $P_c$  and  $P_t$  are the compressor and turbine power respectively as defined by the following equations:

$$W_c = k_c \frac{P_c}{p_1^\mu - 1} \quad (2)$$

$$P_t = \eta_t c_p T_2 \left(1 - \frac{1}{p_2^\mu}\right) W_t \quad (3)$$

Note that  $\mu = 0.286$  and  $k_c$  is a constant parameter, and  $k_t = \eta_t c_p T_2$ . In (3),  $\eta_t$  is the turbine isentropic efficiency

and  $c_p$  the specific heat at constant pressure.

The considered system inputs are:

$$u = \begin{bmatrix} u_1 \\ u_2 \end{bmatrix} = \begin{bmatrix} W_{egr} \\ W_t \end{bmatrix} \quad (4)$$

The considered system outputs are:

$$y = \begin{bmatrix} y_1 \\ y_2 \end{bmatrix} = \begin{bmatrix} p_1 \\ p_2 \end{bmatrix} \quad (5)$$

As suggested in Larsen and Kokotovic (1998), the state variable representation defined by the coordinates reported to the operating point  $(p_{1e}, p_{2e}, p_{ce})$  is carried out. The centered state variables are defined as:

$$\begin{cases} x_1 = p_1 - p_{1e} \\ x_2 = p_2 - p_{2e} \\ x_3 = p_c - p_{ce} \end{cases} \quad (6)$$

while the new control variables are given by:

$$\begin{cases} \tilde{u}_1 = u_1 - u_{1e} \\ \tilde{u}_2 = u_2 - u_{2e} \end{cases} \quad (7)$$

For a desired operating set point defined by a given air fuel ratio  $AFR_e$  and an EGR flow fraction  $EGR_e$ , the choice of the engine speed  $N$  and the fuel command  $W_f$  leads to:

$$\begin{cases} u_{1e} = \frac{EGR_e}{1 - EGR_e} W_{ce} \\ u_{2e} = W_{ce} + W_f \end{cases} \quad (8)$$

In (8),  $W_{ce}$  is expressed:

$$W_{ce} = \frac{W_f}{2} \left[ \delta + \sqrt{\delta^2 - 4(1 - EGR_e)AFR_e} \right] \quad (9)$$

where  $\delta = AFR_e(1 - EGR_e) + 15.6EGR_e - 1$ . and:

$$\begin{cases} p_{1e} = \frac{1}{k_e}(W_{ce} + W_f) \\ p_{2e} = \left[ 1 - \frac{W_{ce}}{W_{ce} + W_f} \frac{1}{k_t k_c \eta_m} (p_{1e}^\mu - 1) \right]^{-\frac{1}{\mu}} \\ p_{ce} = \frac{W_{ce}}{k_c} (p_{1e}^\mu - 1) \end{cases} \quad (10)$$

In the centered coordinates, the nonlinear model is given by:

$$\begin{cases} \dot{x}_1 = -k_1 k_e x_1 - \varphi_1(x_1) + \psi_1(x_1) x_3 + k_1 \tilde{u}_1 \\ \dot{x}_2 = k_2 k_e x_1 - k_2 \tilde{u}_1 - k_2 \tilde{u}_2 \\ \dot{x}_3 = -\frac{1}{\tau} x_3 + \varphi_2(x_2) + \psi_2(x_2) \tilde{u}_2 \end{cases} \quad (11)$$

where the nonlinearities are:

$$\varphi_1(x_1) = \frac{k_1 k_c P_{ce}}{1 - p_{1e}^\mu} \left[ \frac{p_{1e}^\mu - (x_1 + p_{1e})^\mu}{(x_1 + p_{1e})^\mu - 1} \right]$$

$$\psi_1(x_1) = \frac{k_1 k_c}{(x_1 + p_{1e})^\mu - 1}$$

$$\varphi_2(x_2) = \frac{P_{ce}}{\tau} \left[ \frac{p_{2e}^{-\mu} - (x_2 + p_{2e})^{-\mu}}{1 - p_{2e}^{-\mu}} \right]$$



So, it is possible to apply to the system (13) the feedback law:

$$u(k) = \Delta_1^{-1}(\nu(k) - \Delta_0 x(k)) \quad (24)$$

where  $\nu(k)$  is the input of the decoupled system. Let the decoupled system be given by the new representation:

$$\begin{cases} x(k+1) = \bar{A}x(k) + \bar{B}\nu(k) \\ y(k) = Cx(k) \end{cases} \quad (25)$$

where  $\bar{A} = A - B\Delta_1^{-1}\Delta_0$  and  $\bar{B} = B\Delta_1^{-1}$ . Note also that the system is finally decoupled in  $s$  independent chains of integrators as shown in (Fig. 2).

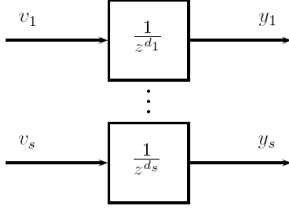


Fig. 2. Chains of decoupled input-output subsystems

#### 4.2 Base-change Matrices

The system having now been decoupled, it is possible to fix independently dynamics of the various input-output chains. With this intention, a base-change is carried out:

$$\begin{cases} \xi(k+1) = \begin{bmatrix} \xi_1(k+1) \\ \vdots \\ \xi_s(k+1) \end{bmatrix} = T x(k+1) \end{cases} \quad (26)$$

so that:

$$\begin{cases} \xi(k+1) = \begin{bmatrix} A_1 & & \\ & \ddots & \\ & & A_s \end{bmatrix} \xi(k) + \begin{bmatrix} \beta_1 & & \\ & \ddots & \\ & & \beta_s \end{bmatrix} \nu(k) \\ y(k) = \begin{bmatrix} \gamma_1 & & \\ & \ddots & \\ & & \gamma_s \end{bmatrix} \xi(k) \end{cases} \quad (27)$$

with

$$T = \begin{bmatrix} c_1 \\ c_2 \\ \tau \end{bmatrix} \quad (28)$$

The new state-space representation is now expressed in the new base by the following equations:

$$\begin{cases} \xi(k+1) = \tilde{A}\xi(k) + \tilde{B}\nu(k) \\ y(k) = \tilde{C}\xi(k) \end{cases} \quad (29)$$

with

$$\begin{aligned} \tilde{A} &= T\bar{A}T^{-1} \\ \tilde{B} &= T\bar{B} \\ \tilde{C} &= \bar{C}T^{-1} \end{aligned}$$

where every triplet  $(A_i, \beta_i, \gamma_i)$  is given in the controllable canonical form.

#### 4.3 Dynamic Modification of The Decoupled System

The determination of gain  $\tilde{K}_i$  (associated to the  $i^{th}$  subsystem) by pole placement and the deduction of coefficients of the characteristic polynomial

$$\Phi(z) = z^{d_i} + \alpha_{id_{i-1}}z^{d_i-1} + \dots + \alpha_{i0} \quad (30)$$

leads to the new control law:

$$\nu(k) = -\tilde{K}\xi(k) + y_c = -\tilde{K}Tx(k) + y_c = -Kx(k) + y_c \quad (31)$$

with

$$K = \begin{bmatrix} \alpha_1 & & \\ & \ddots & \\ & & \alpha_s \end{bmatrix} \quad (32)$$

and

$$\alpha_i = [\alpha_{i0} \ \alpha_{i1} \ \dots \ \alpha_{id_{i-1}}] \quad (33)$$

The combination of the decoupling technique with equation (31) transforms the control equation into:

$$u = -\Delta_1^{-1}(\Delta_0 + \tilde{K}T)x + \Delta_1^{-1}y_c \quad (34)$$

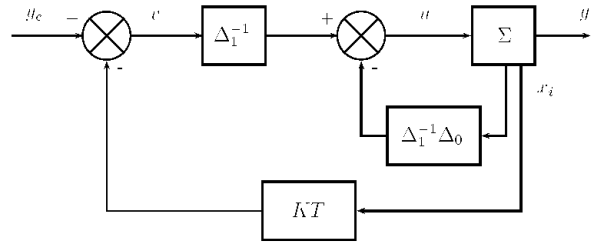


Fig. 3. Stabilization of the decoupled MIMO system

If  $\check{d} = \sum d_i = n$ , the closed-loop control system shown in (Fig. 3) and the system (13) have same orders. The process (25) is thus observable and controllable.

In the opposite case ( $\check{d} < n$ ) the system (25) cannot represent the totality of the system (13) and the zero dynamics are stabilized. There are then  $(n - \check{d})$  unobservable modes. It is thus important to highlight them (by an adequate base-change) before carrying out the pole placement.

According to the nature of the system modes, the control law  $u$  is calculated to modify the observable or unobservable modes with or without destroying the interaction between the control laws  $u_i$ .

#### 4.4 Finding Prediction Matrices

Once the system has been stabilized, the following stage consists in establishing the predictive control for all of the obtained Simple-Input, Simple-Output (SISO) subsystems.

The criterion to be minimized is:



at  $t = 25s$ , it is not capable of preserving dynamic and steady-state performance.

Simulation results shown in (Fig. 7) and (Fig. 8) have been obtained by applying the GPC decoupled approach with the adequate increment weighting and horizons. The fault occurrence is starting from  $t = 25s$ . Figures (Fig. 7) and (Fig. 8) show explicitly the convergence of the different outputs of the system considered as decoupled. After the fault has been identified, Nourah and C. Fonte (1993), the accommodation method updates the state estimator and the controller structure.

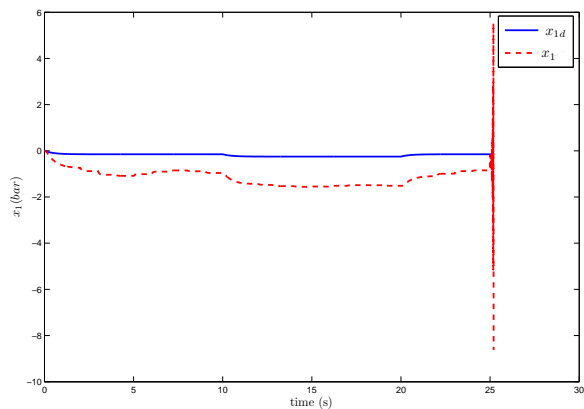


Fig. 5.  $x_1$  (bar) vs time(s)

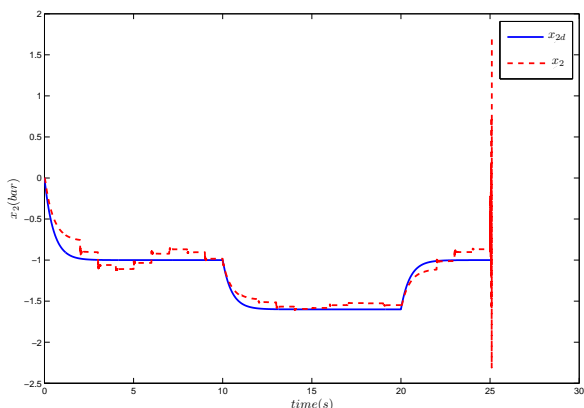


Fig. 6.  $x_2$  (bar) vs time(s)

## 6. CONCLUSIONS AND FUTURE WORKS

### 6.1 Conclusions

In this paper, a fault-tolerant predictive control strategy is proposed. It combines the state-based GPC approach with indirect failure accommodation. Under the hypothesis that the considered system can be decoupled, the controller gives considerably better performance. The proposed method deals with the closed loops of the various subsystems separately. On the one hand, it fixes independently the dynamics of each subsystem and offset the unstable zeros with decoupling law. As a result, it is

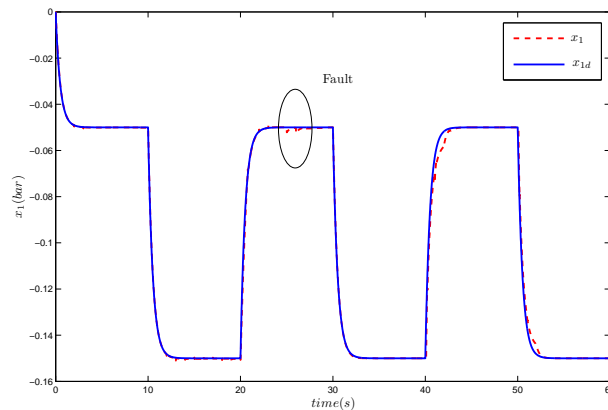


Fig. 7.  $x_1$  (bar) vs time(s)

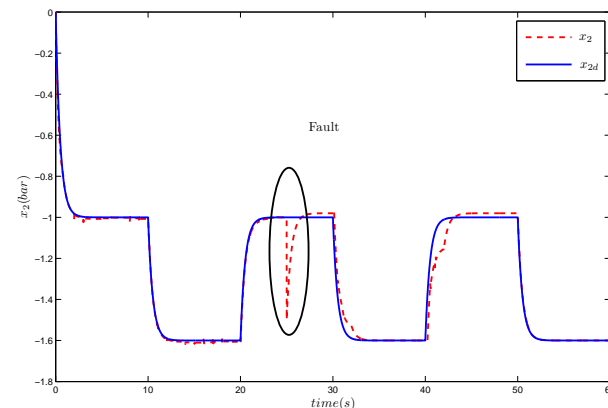


Fig. 8.  $x_2$  (bar) vs time(s)

particularly recommended for unstable multivariable non-minimum phase systems. On the other hand, it makes it possible to optimize separately the choice of the GPC parameters for each subsystem. Finally, the use of an adaptive state-observer permits the controller to accommodate actuator or /and system failures.

Applied to the model of the Diesel engine air system, the resulting predictive controller exhibits good performance in terms of trajectory tracking when a fault occurs.

### 6.2 Future Works

Future work will consist in applying this method to a Caterpillar six-cylinder Diesel engine (3126B).

## ACKNOWLEDGEMENTS

The authors gratefully acknowledge the contribution of the European Union supporting to the PACTE (Prototyping of Advanced Control Techniques for Engines) project within the framework of the INTERREG III programme.

## REFERENCES

- O. Bego, N. Peric, and I. Petrovic. Decoupling multivariable gpc with reference observation. *Proceedings of the 10th Mediterranean Electrotechnical Conference - MELECON 2000, Cyprus*, pages 819 – 822, 2000.

- M.E.H. Benbouzid, D. Diallo, and M. Zeraouia. Advanced fault-tolerant control of induction-motor drives for ev/hev traction applications: From conventional to modern and intelligent control techniques. *IEEE Vehicular Technology Society*, 56:519 – 528, 2007.
- J. Chen and R. J. Patton. *Robust Model-based Fault Diagnosis for Dynamic Systems*. Klumer Academic Publishers, 1999.
- H Demircioglu and E Karasu. Generalized predictive control. a practical application and comparison of discrete- and continuous-time versions. *IEEE Cont. Sys. Mag*, pages 36–43, 2000.
- A L Elshafei, G Dumont, and A Elnaggar. Perturbation analysis of gpc with one-step control horizon. *Automatica (Journal of IFAC)*, 27:725–728, 1991.
- M Fliess and R Marquez. Towards a module-theoretic approach to discrete-time linear predictive control. *14th ISMTNS*, 2000.
- A.J Fossard. Systèmes multi-entrées-multi-sorties. *Techniques de l'Ingénieur*, R7 220, 1997.
- P J Gawthrop. Linear predictive pole placement control : practical issues. *Proceedings of the 39th IEEE Conference on Decision and Control*, 1:160–165, 2000.
- K Guemghar, B Srinivasan, and D Bonvin. Control of pendubot using input-output feedback linearization and predictive control. *IFAC*, 2005.
- M. Huzmezan and J. Maciejowski. Reconfigurable control methods and related issues - a survey. Technical report, Technical report prepared for the DERA under the Research Agreement no. ASF/3455, Department of Engineering, 1997.
- M.J. Jankovic, M.I. Jankovic, and I. Kolmanovsky. Constructive lyapunov control design for turbocharged diesel engines. *IEEE Trans. on Control Systems Technology*, 8:288–299, 2000.
- M. Larsen and P. Kokotovic. Passivation design for a turbocharged diesel engine model. *Decision and Control*, 2:1535 – 1540, 1998.
- K. N. Layerle, N. Langlois, and H. Chafouk. Synthèse de contrôleurs prédictifs à base d'état pour la commande des systèmes mimo discrets à non-minimum de phase. *8 th conference STA '2007, ACS 170, 05 to 07 november 2007 at Soussein Tunisia*, 2007.
- K W Lim, W K Ho, T H Lee, K V Ling, and W Xu. Generalised predictive controller with pole restriction. *IEE Proceeding Control Theory*, 145:219–225, 1998.
- D. P. Looze, J. L. Weiss, J. S. Eterno, and N. M. Barrett. An automatic redesign approach for restructurable control systems. *IEEE Control System Magazine*, pages 16–22, 1985.
- D. Q. Mayne, J. B. Rawlings, C. V. Rao, and P. O. M. Scokaert. Constrained model predictive control: Stability and optimality. *Automatica*, 36:789–814, 2000.
- H. Noura, D. Sauter, and C. Aubrun. A fault detection and accommodation method applied to an inverted pendulum. *Control Applications, 1994., Proceedings of the Third IEEE Conference on*, 2:1397 – 1402, 1994.
- H. Nourah and M. Robert C. Fonte. Fault tolerant control using simultaneous stabilization. *Conference Proceedings*, 3:605 – 610, 1993.
- R. J. Patton. Fault-tolerant control: The 1997 situation. *IFAC Fault Detection, Supervision and Safety for Technical Processes*, pages 1029–1051, 1997.
- Alexandros Plianos, Ali Achir, Richard Stobart, Nicolas Langlois, and Houcine Chafouk. Dynamic feedback linearization based control synthesis of the turbocharged diesel engine. *American Control Conference*, pages 4407 – 4412, 2007.
- S Qin and T Badgwell. A survey of industrial model predictive control technology. *Control Engineering Practice*, 11:733–764, 2003.
- N L Ricker. Model predictive control : state of the art. *4 th International Conference on Chemical Process Control*, pages 271–296, 1991.
- I Santro, I Peric, and I Petrovii. Comparison of the self-tuning generalized predictive controller and pole placement controller. *Proceedings of the 9th MEC*, pages 539–543, 1998.
- D. Sauter, F. Hamelin, and H .Noura. Fault diagnosis and accommodation in dynamic systems; application to a dc motor. *American Control Conference, 1998. Proceedings of the 1998*, 5:2872 – 2873, 1998.
- I Skrjanc, S Blazic, S Oblak, and J Richalet. An approach to predictive control of multivariable time-delayed plant: stability and design issues. *ISA Trans*, 43:585–595, 2004.
- L Wang and Peter C Young. An improved structure for model predictive control using non-minimal state space realisation. *Journal of Process Control*, 16:355–371, 2006.
- K Watanabe, K Ikeda, T Fukuda, and S G Tzafestas. Adaptive generalized predictive control using a state-space approach. *IEEE RSJ*, pages 1609–1614, 1991.